The Topology of Politics

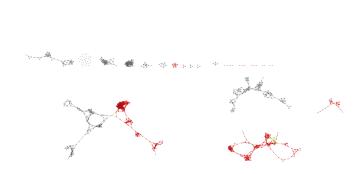
Mikael Vejdemo-Johansson

School of Computer Science University of St Andrews Scotland

October 26, 2011



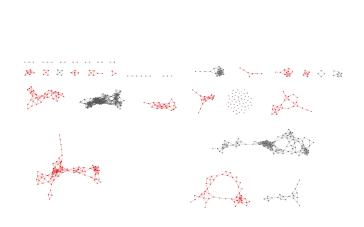
Southern Democrats





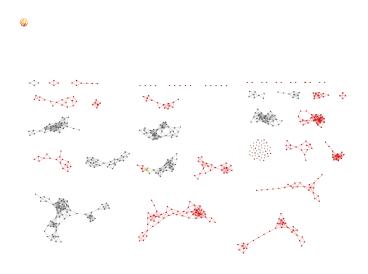
26 October 2011

Obama wins





Health care reform





26 October 2011

Outline

Data analysis

Data analysis in politics

Wherefore topology?

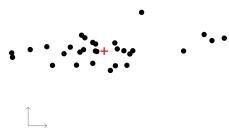




Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Mean (centroid) tells us where the data is located.

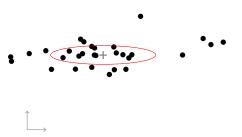




Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Standard deviation tells us how spread out the data is.

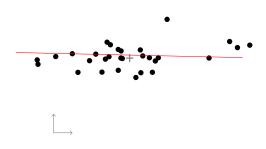




Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Regression analyses fit the data to an easy to analyze model.

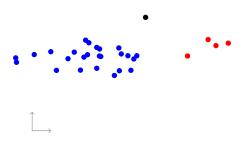




Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Cluster analysis divides the data into its connected components.





Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Principal Component Analysis (and other dimension reduction techniques) give new coordinates that more faithfully represent the data.







Outline

Data analysis

Data analysis in politics

Wherefore topology?





Data analysis has long pedigree in political science.

- Tufte discusses improvements to techniques in a 1969 paper
- Gallups, polling, and voter prediction leverages more and stronger analysis techniques every year.

Entered into politics in the 90's. Example of the type of analyses done: PCA of votes in House of Congress.





We shall focus on one area of use: the analysis of parliamentary bodies.

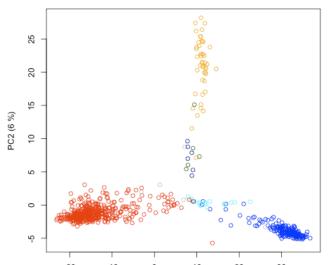
Dataset

For a parliamentary session, N members of parliament vote on M issues. Votes form an $N \times M$ -matrix V of votes cast. Encoded +1 for Yea, -1 for Nay and 0 for all other results.

c.f. Dan Rockmore's work using similarly constructed datasets.

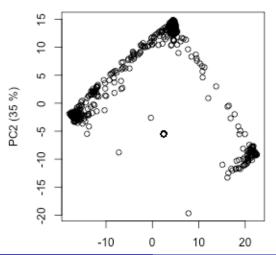
















Outline

Data analysis

Data analysis in politics

Wherefore topology?





Wherefore topology?

Topology gives qualitative information

Topology is about geometric properties not dependent on a metric: How many pieces? Are there holes? Bubbles? Can you get turned around while moving?

Topology captures continuity, connectedness, nearness

In particular, the non-dependence on a metric helps if metrics are ill-motivated, eg phylo-genetics.





A topological analysis method

In a recent PhD thesis at Stanford [Singh, '08], a topological method for data analysis was introduced.

Fundamental topological result: Nerve lemma

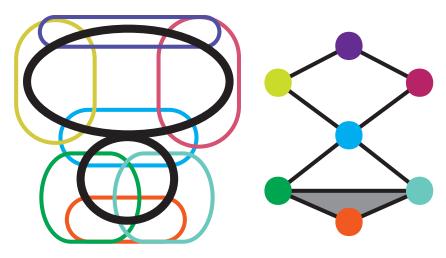
Suppose a space X is subdivided $X = \bigcup_i X_i$ into *contractible* (read simple) components.

Then *X* is equivalent to the *nerve* of the covering.



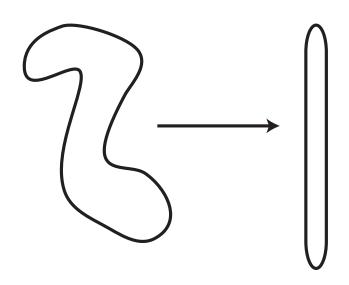


The nerve of a covering



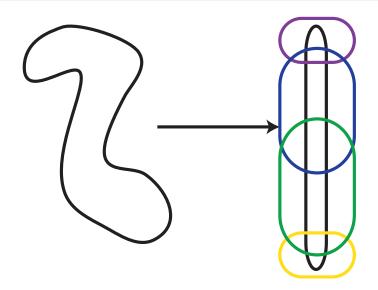






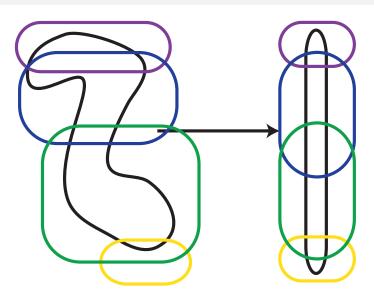






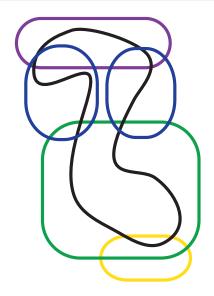






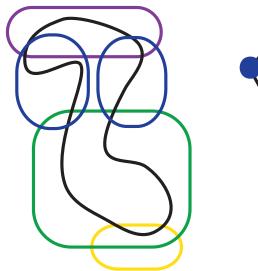


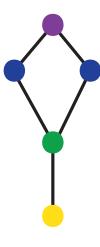














Translate topology to statistics

Continuous function
Covering of target space
Preimages
Connected components
Nerve complex

Measurement function on datapoints

Covering of datapoints

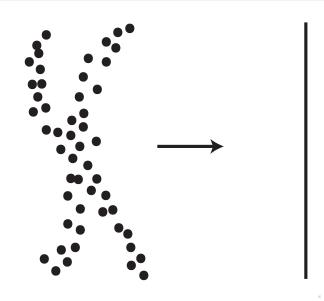
Preimages

Clusters

Mapper diagram

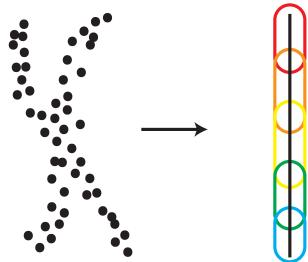






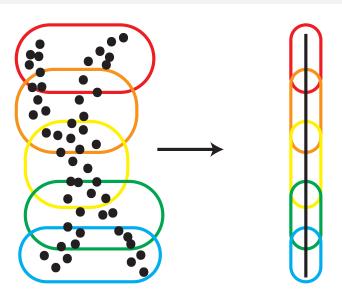






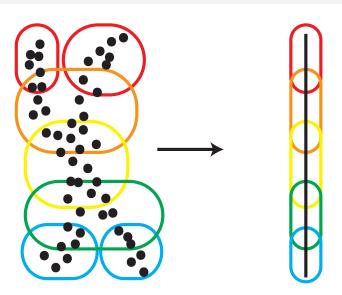






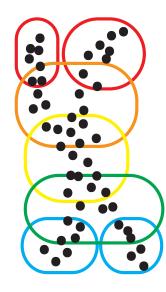


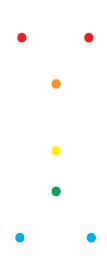




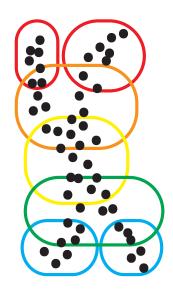


















Implementation

This method is provided in a software package currently marketed by Ayasdi.

Startup company founded by Gurjeet Singh (original thesis on Mapper) and Gunnar Carlsson (thesis advisor).

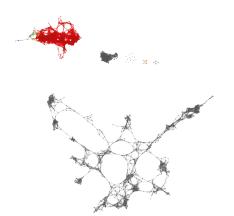






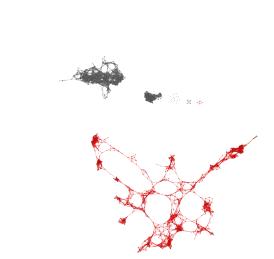
Parliamentary period 2001–2005. Conservative







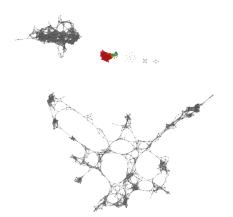
Parliamentary period 2001–2005. Labour





Parliamentary period 2001–2005. Liberal Democrats

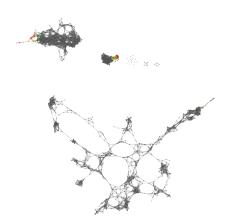






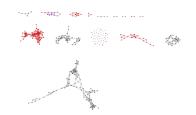
Parliamentary period 2001–2005. Regional parties

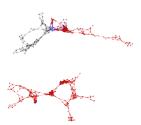
























1993





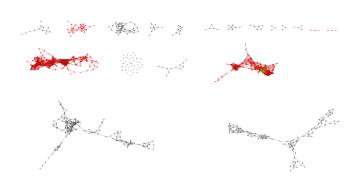
26 October 2011





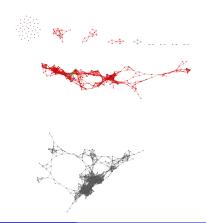












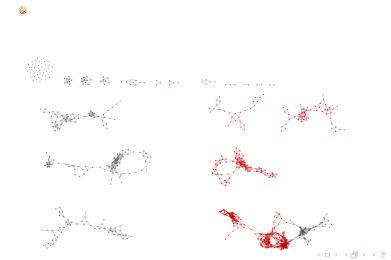






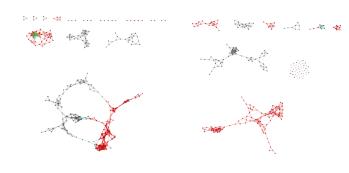






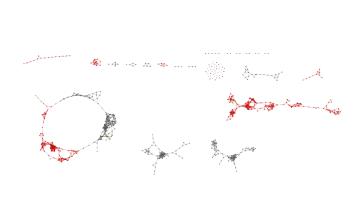








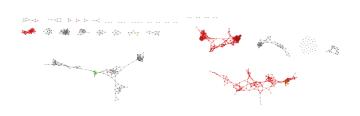
2000





26 October 2011





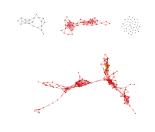


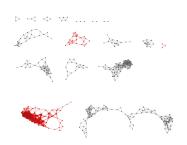




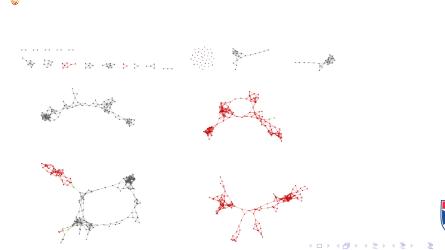




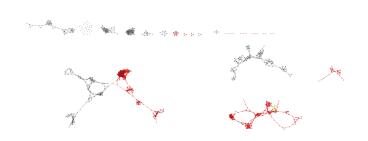




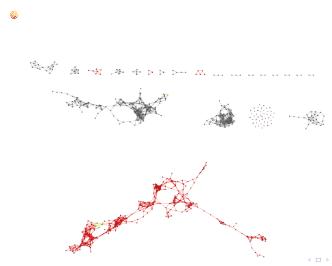




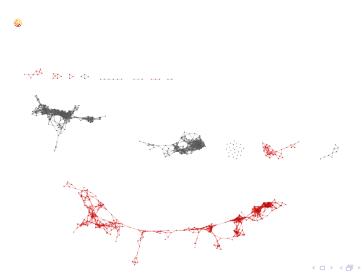




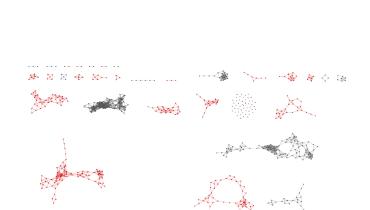








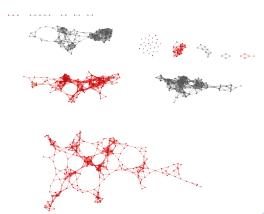




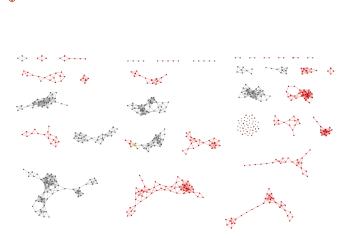














Questions?

Future directions

- More parliaments. We have (mostly un-analyzed) data for:
 - Sweden
 - European Union
 - Canada
 - US Senate
- Network analysis: who co-sponsors with whom, what are the parliamentary cliques?
- Meme spread: who takes over turns of phrase from whom?



